

KNOW	/ 12	APP	/ 12	INQ	/ 12	COMM	/ 6
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MCV4UP - UNIT 7 – THE DEFINITE INTEGRAL

TEST

GIVE ALL ANSWERS IN EXACT FORM, UNLESS STATED OTHERWISE.

PART A – This section is to be completed without the use of a calculator. Upon completing this section, hand it in to receive the remainder of the test.

1) Evaluate each of the following. (*K – 2 marks each*)

a) $\frac{d}{dx} \int_5^x \frac{11t}{2t^3 + 7} dt$

b) $\int_1^3 (3x^2 - 4x + 1) dx$

c) $\int_{-2}^{-1} \frac{2}{x^2} dx$

d) $\int_0^{\pi} (1 + \cos x) dx$

e) $\frac{d}{dx} \int_{3x^2}^7 \sqrt{3t^4 + t - 8} dt$

f) $\frac{d}{dx} \int_{\sin x}^{\cos x} t^2 dt$

PART B – This section may be completed with the use of a calculator.

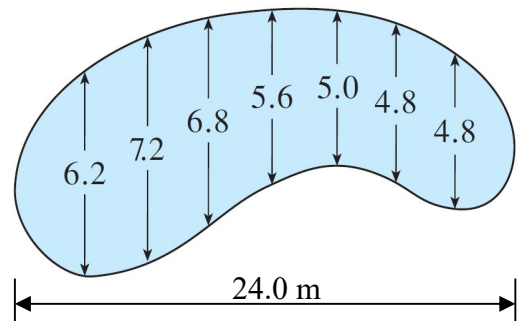
NAME: _____

- 2) By hand, use RRAM with 4 equal subintervals to estimate the area between the curve $f(x) = \sqrt{x} + 4$ and the x -axis on the interval $3 \leq x \leq 5$, to the nearest tenth. (*A – 3 marks*)

Time (s)	Velocity (m/s)
0	0
0.5	4.67
1.0	7.34
1.5	8.86
2.0	9.73
2.5	10.22
3.0	10.51

- 3) A radar gun was used to record the speed of a runner during the first 3 seconds of a race, as shown in the table to the left. Use the Trapezoidal Rule to estimate the distance the runner covered during those 3 seconds, to the nearest tenth. (*A – 3 marks*)

- 4) The widths (in metres) of a kidney-shaped swimming pool were measured as indicated in the figure on the right. Use Simpson's Rules to estimate the area of the pool's surface to the nearest tenth. (*A – 3 marks*)



- 5) The linear density in a rod 8 m long is $\frac{12}{\sqrt{x+1}}$ kg/m, where x is measured in metres from one end of the rod. Without using a calculator program, determine the average density of the rod. (*A – 3 marks*)

- 6) A sphere is created by rotating a circle with equation $x^2 + y^2 = 36$ around the x -axis. In order to create a hemisphere, only the positive x -values are used.
- a) Without the use of a calculator program, use LRAM with 3 equal subintervals to estimate the volume of the hemisphere to the nearest tenth. (*1 – 4 marks*)

b) If using a calculator program to estimate the volume of the hemisphere, what function should be entered into the calculator? (*1 – 1 mark*)

c) Using a calculator program to compute MRAM with 100 subintervals, estimate the volume of the hemisphere to the nearest tenth. (*1 – 1 mark*)

- 7) Determine, to the nearest tenth, the total area between the curve $f(x) = -6x^2 + 54$ and the x -axis on the interval $[1, 5]$. Show all work leading to the final answer. (*1 – 3 marks*)

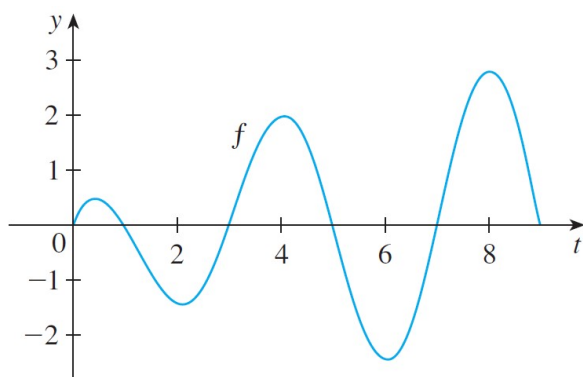
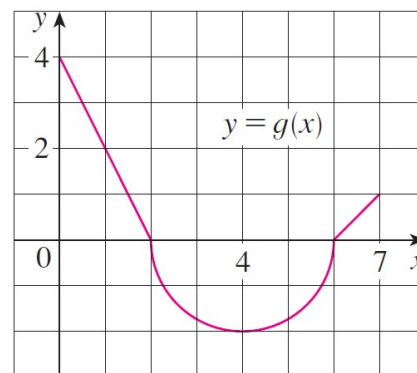
8) Use a calculator program to evaluate $\int_{-1}^{10} \frac{x^2 - 3}{7x + 8} dx$ to the nearest tenth. (*1 – 1 mark*)

9) Without using a calculator's integration function, evaluate $\int_3^7 \frac{10x}{x^2 + 3} dx$ to the nearest tenth.

Show all work leading to the final answer. (*1 – 2 marks*)

- 10) The graph of $y = g(x)$ shown on the right consists of two straight lines and a semicircle. Use the graph to evaluate

$$\int_0^7 g(x) dx \text{ to the nearest tenth. (C - 2 marks)}$$



- 11) Let $g(x) = \int_0^x f(t) dt$, where f is the function whose graph is shown on the left.

a) On what intervals is $g(x)$ decreasing? (C - 1 mark)

b) Is $g(3)$ positive or negative? (C - 1 mark)

- 12) Let $f(x) = 3x^2 - 4$.

a) What value does the Mean Value Theorem for Definite Integrals guarantee that $f(x)$ will equal on the interval $[0, 4]$? (C - 1 mark)

b) At what x -value does the function assume the value found in part (a)? Express your answer in exact form. (C - 1 mark)